

# Reconciling Eventually-Consistent Data with CRDTs

Starring **Noel Welsh**

A **mynna** Production

In conjunction with  
**\_.underscore**

Showing at

**Scala eXchange 2013**





**Why are we  
here?**



# CRDTs

**(An overview)**

# **Conflict-free Replicated Data Type**

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# Conflict-free Replicated Data Type

# **Conflict-free** **Replicated** **Data Type**



**Conflict-free**  
**Convergent**  
**Commutative**

**Merge data**  
**automatically**

#1

Scala

#2

# Abstract Algebra

#3

# Special Relativity

**Why do we  
care?**



**You have an  
awesome  
web site**

**So you want**  
**sub-Second**  
**page load**

# Use **Scala**

Spray: >200K requests/s

Rails: 4640 requests/s

Source: Tech Empower JSON serialization benchmark

<http://www.techempower.com/benchmarks/>

**That's**  
**not**  
**enough**



$$E=Mc^2$$





World map from Wikimedia Commons



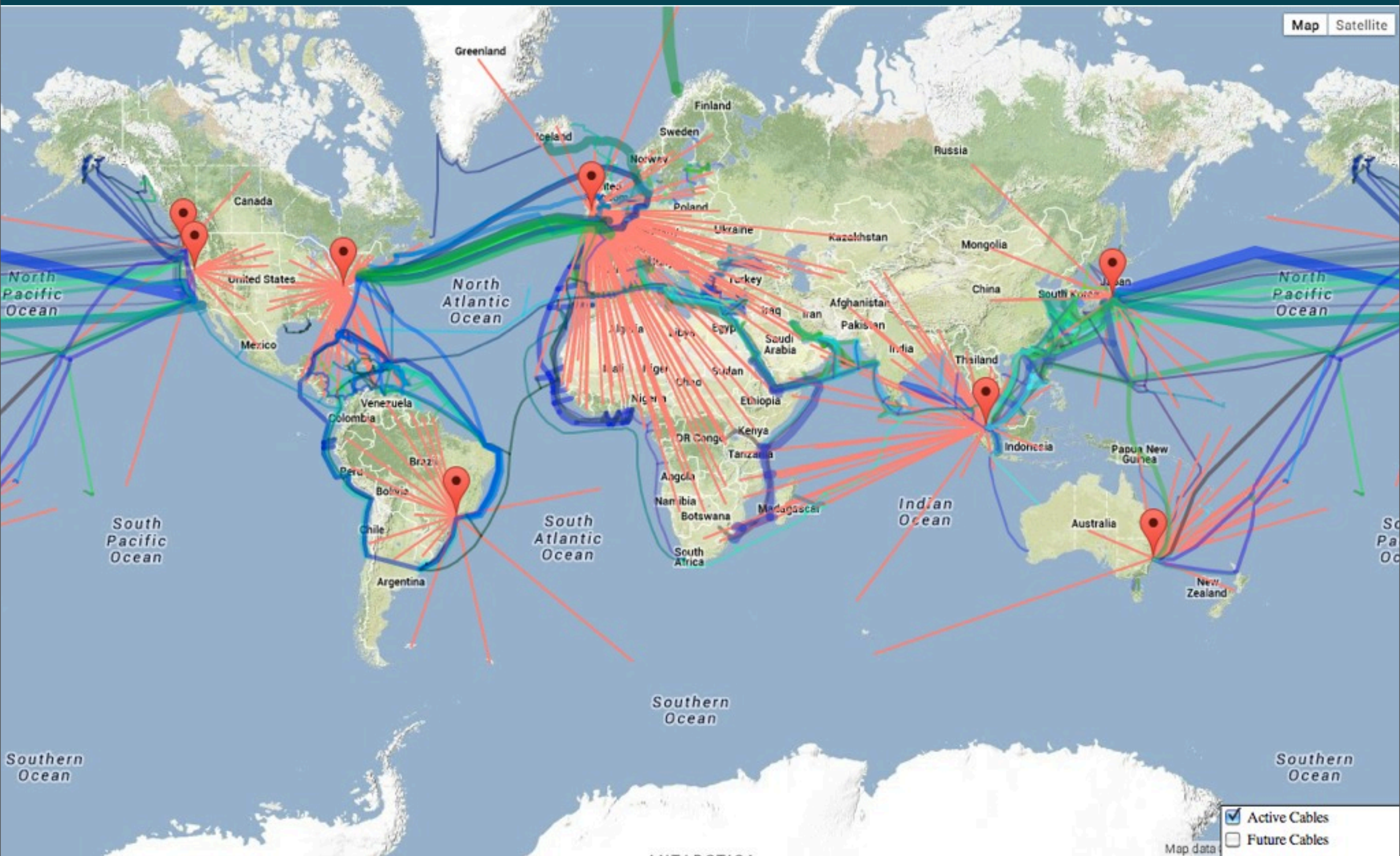
<http://www.flickr.com/photos/21561428@N03/5185781936/>

**LOCATION**

**LOCATION**

**LOCATION**



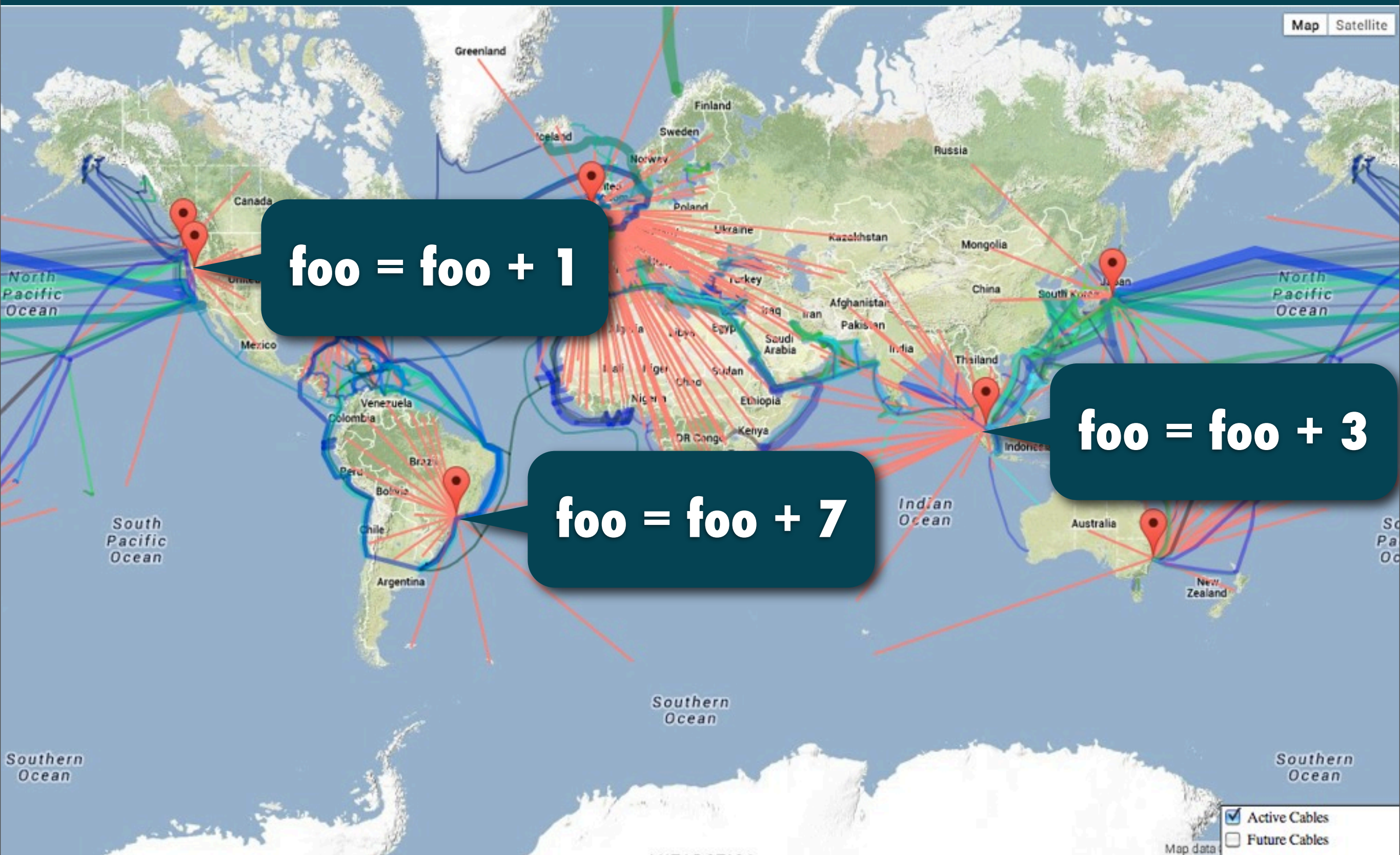


<http://turnkeylinux.github.io/aws-datacenters/>

**Problem**  
**SOLVED!**

**Problem**  
**SOLVED?**





<http://turnkeylinux.github.io/aws-datacenters/>

**What the FOO?**

$(0,0,0)$

$\text{foo} = \text{foo} + 1$

$(1,0,0)$

$(1,1,0)$

$(1,0,1)$

$(1,1,1)$

...

$\text{foo} = \text{foo} + 7$

$(1,7,0)$

$(1,7,7)$

**We have conquered**

**Latency**

**We have lost**

**Consistency**

# Solution #1 (Quantum Mechanics)

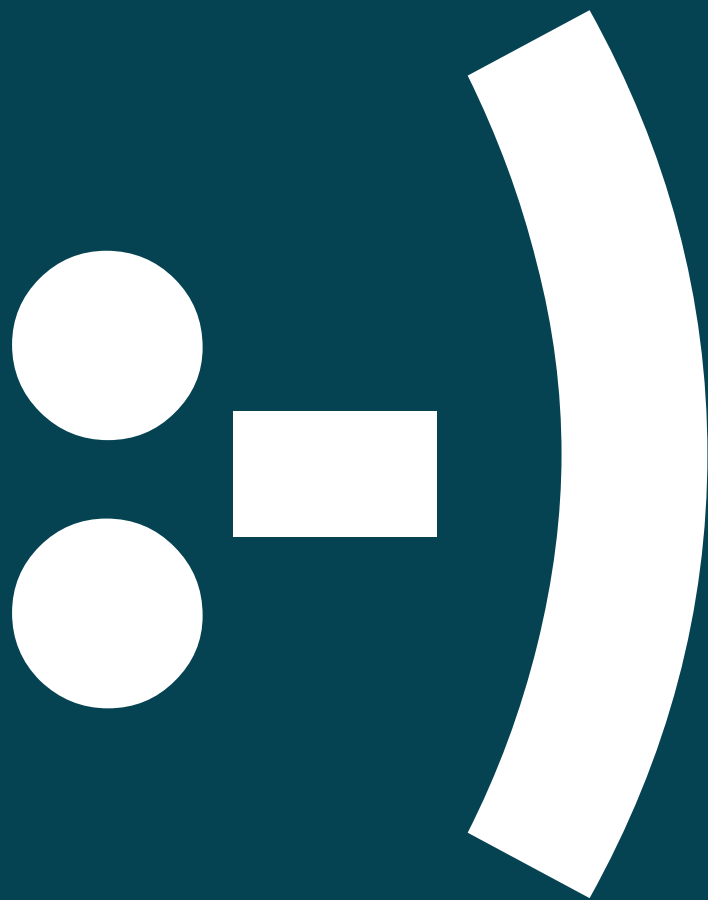
Simply consider all possible world states and ...





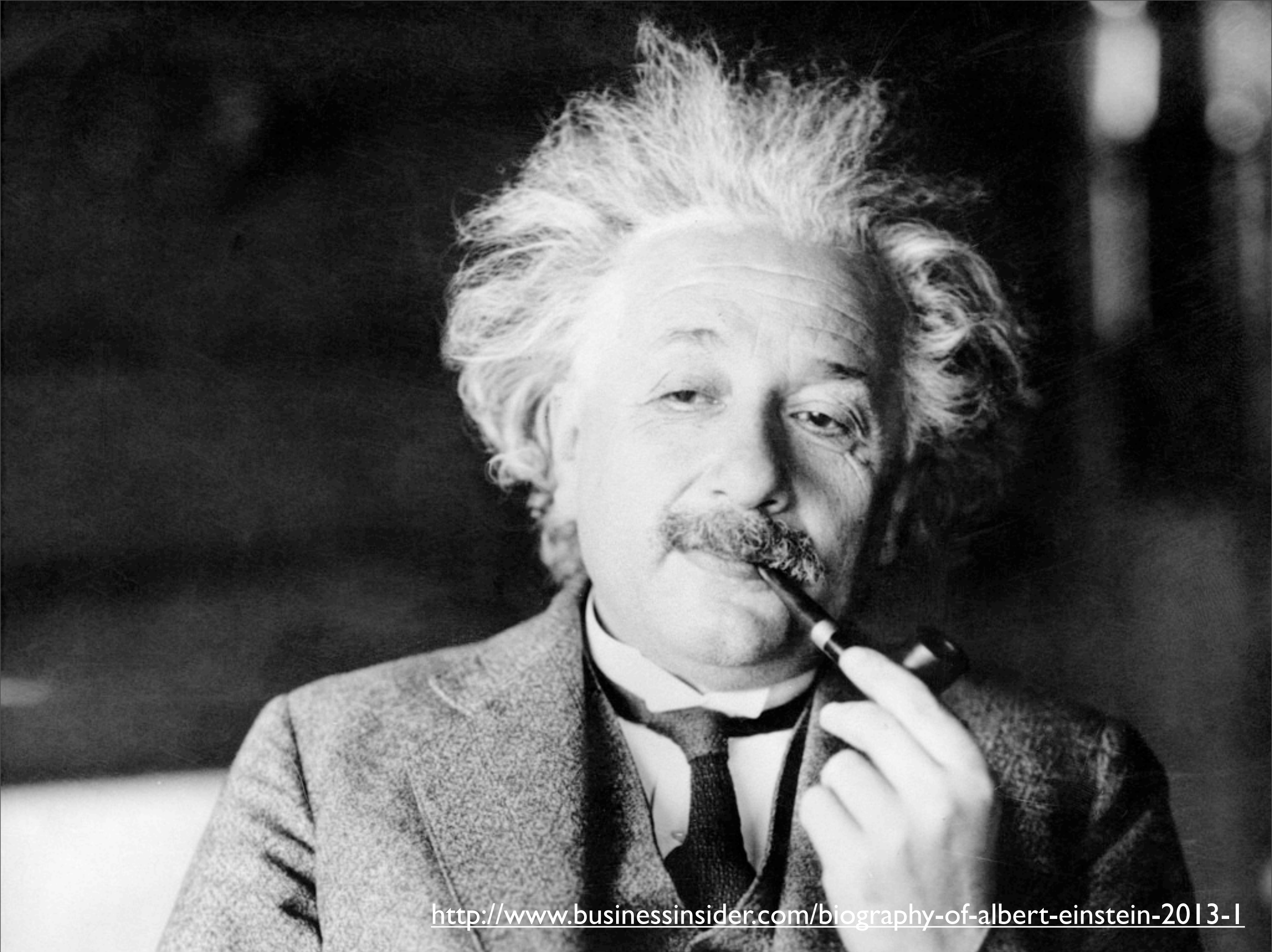
# Solution #2 (Google)

Simply use atomic clocks to establish temporal ordering of events and distributed transactions ...



# Solution #3 (Special Relativity)

Simply trade time for space!



<http://www.businessinsider.com/biography-of-albert-einstein-2013-1>

# G-Counter

**A counter that can  
only GROW**

**G-Counter insight:  
Store a separate  
counter for each  
machine**

# G-Counter

Machine A

A:0

B:0

Machine B

A:0

B:0



**A machine can only  
increment its own  
counter**

# G-Counter

Machine A

A:5

B:0

Machine B

A:0

B:7

**Merge is simply the**  
**max**

# G-Counter

Machine A

A:5

B:7

Machine B

A:5

B:7

**The counter's value  
is simply the  
total**

# G-Counter

Machine A

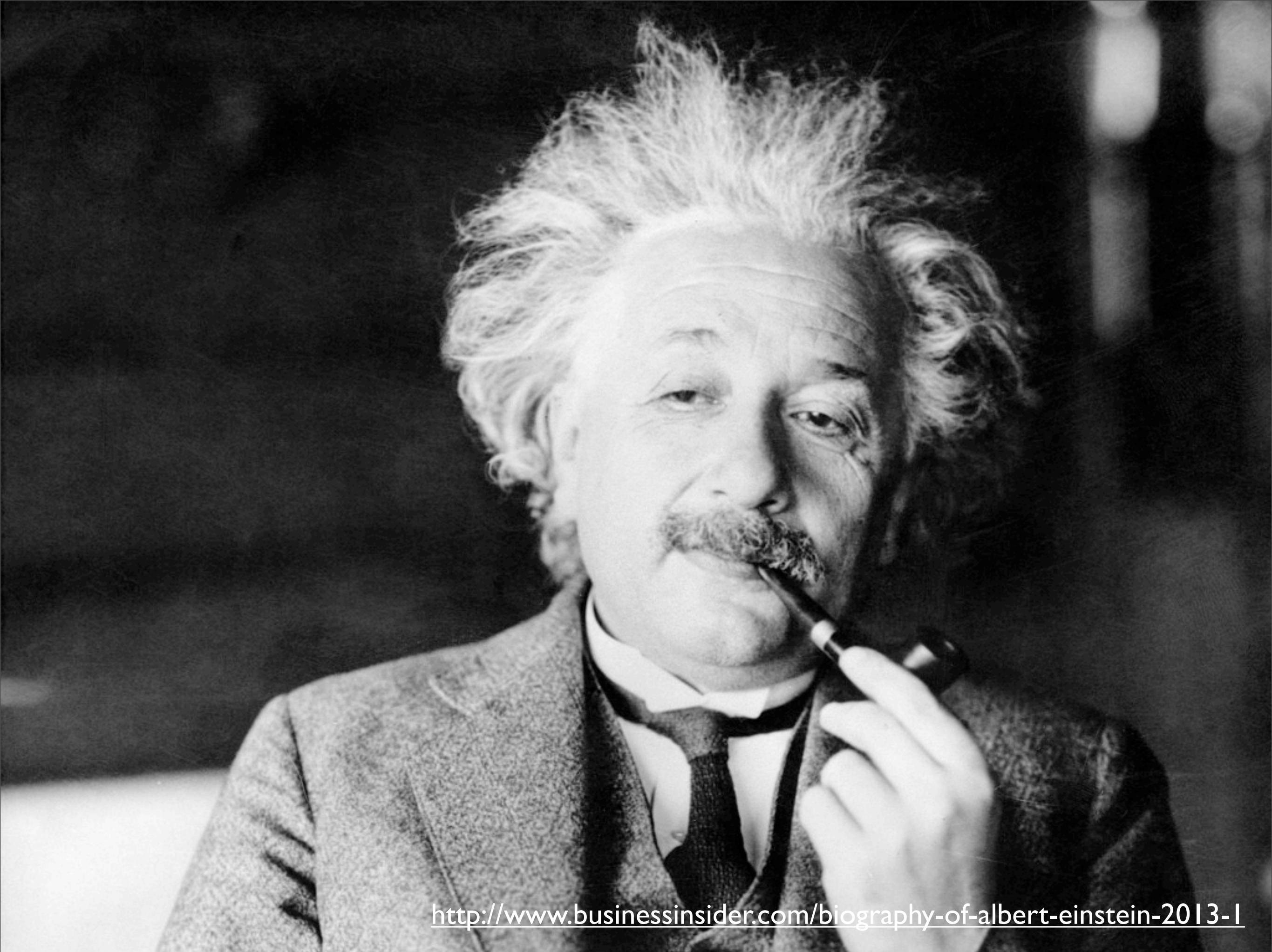
Machine B

A: 5 Total A: 5  
B: 7 is 10 B: 7

**We have a**  
**distributed**  
**eventually-consistent**  
**increment-only**  
**counter**

**We have used**  
**space** to become  
invariant to **time**





<http://www.businessinsider.com/biography-of-albert-einstein-2013-1>

**Can we abstract  
this idea?**

```
trait GCounter[Id, Elt] {  
  
  def inc(id: Id, amt: Elt)  
  
  def total: Elt  
  
  def merge(c: GCounter[Id,  
Elt]): GCounter[Id, Elt]  
  
}
```

**total** requires **Elt** has +

**inc** requires **Elt** has +,0

**+ must be**

**Invariant to  
order**

# Formally: Associative

$$(x \bullet y) \bullet z = x \bullet (y \bullet z)$$

# Formally:

# Commutative

$$x \bullet y = y \bullet x$$

# **A Commutative Monoid!**







```
def inc(id: Id, amt: Elt)  
  (implicit m: Monoid[Elt])
```

```
def total(implicit m:  
Monoid[Elt]): Elt
```

**merge** requires

**Elt** has **max**

**max must be**  
**Invariant to**  
**order**

# Formally:

# Associative

$$(x \bullet y) \bullet z = x \bullet (y \bullet z)$$

# Formally:

# Commutative

$$x \bullet y = y \bullet x$$

**max must**

**Converge to the  
correct value**



# Formally: Idempotent

$$x \bullet x = x$$

**An Idempotent  
Commutative  
Monoid!!!!**

```
def merge(c: GCounter[Id,  
Elt])(implicit m: Monoid[Elt  
@@ Max]): GCounter[Id, Elt]
```

**Number (+)**

**Number (\*)**

**Tuple**

**Map**

**Option**

**Average**

**Moving average**

**t-digest**

**Set (intersection)**

**Set (union)**

**Hyperloglog**

**Bloom filter**

**Count-min**

**Vector**

**Q-Tree**

**SGD**

# G-Set

Machine A

$A:\{x\}$

$B:\{\}$

Machine B

$A:\{\}$

$B:\{y,z\}$

# G-Set Merge

Machine A

A: {x}

B: {y, z}

Machine B

A: {x}

B: {y, z}

# G-Set Total

Machine A

Machine B

Set is

$A:\{x\}$

$B:\{y,z\}$

$\{x,y,z\}$

# PN-Counter



**A counter that can**  
**GROW** and  
**SHRINK**

**Can't use a G-  
Counter as we can't  
use max to merge**

**Use**  
**Two**  
**G-counters!**

# PN-Counter

Machine A

Additions

A: 4, B: 2

Subtractions

A: 5, B: 3

Machine B

Additions

A: 4, B: 7

Subtractions

A: 3, B: 4

**Merge is simply the**  
**MAX**

# PN-Counter

Machine A  
Additions

A: 4, B: 7

Subtractions

A: 5, B: 4

Machine B  
Additions

A: 4, B: 7

Subtractions

A: 5, B: 4

**The counter's value  
is simply the  
TOTAL**

# PN-Counter

Machine A

Additions

A: 4, B: 7

Subtractions

A: 5, B: 4

Machine B

Additions

A: 4, B: 7

Subtractions

A: 5, B: 4

Total is

$$(4+7) - (5+4) =$$

2



```
trait PNCOUNTER[Id, Elt] {  
  def inc(id: Id, amt: Elt)  
  def dec(id: Id, amt: Elt)  
  def total: Elt  
  
  def merge(c: GCounter[Id, Elt]):  
    GCounter[Id, Elt]  
}
```

**PN-Counter requires**  
**Elt** has addition,  
**zero, and**  
**subtraction**

# **A Commutative Group!**

```
trait PNCOUNTER[Id, Elt] {  
  def inc(id: Id, amt: Elt)(implicit m: Monoid[Elt])  
  
  def dec(id: Id, amt: Elt)(implicit m: Monoid[Elt])  
  
  def total(implicit m: Group[Elt]): Elt  
  
  def merge(c: GCounter[Id, Elt])(implicit m: Monoid[Elt @@ Max]): GCounter[Id, Elt]  
}
```

**Numbers are clearly  
a commutative  
group**

**Sets with union and  
set difference are a  
commutative group**

# PN-Set

# 2P-Set

Machine A  
Additions

A: {x}, B: {y}

Subtractions

A: {x}, B: {}

Machine B  
Additions

A: {x}, B: {y, z}

Subtractions

A: {}, B: {y}



# 2P-Set Merge

Machine A  
Additions

A: {x}, B: {y, z}

Subtractions

A: {x}, B: {y}

Machine B  
Additions

A: {x}, B: {y, z}

Subtractions

A: {x}, B: {y}

# 2P-Set Total

Machine A

Additions

A: {x}, B: {y, z}

Subtractions

A: {x}, B: {y}

Machine B

Additions

A: {x}, B: {y, z}

Subtractions

A: {x}, B: {y}

Set is  
{z}

**Deleted elements  
stored indefinitely.**

**Called**

**tombstones**

**2P-Set allows  
elements to be  
added and removed  
once**

# C-Set

## Store element and count

# C-Set

Machine A

Additions

A:  $\{(x, 2)\}$ ,

B:  $\{(y, 1)\}$

Subtractions

A:  $\{(x, 1)\}$ ,

B:  $\{\}$

Machine B

Additions

A:  $\{(x, 1)\}$ ,

B:  $\{(y, 1), (z, 2)\}$

Subtractions

A:  $\{\}$ ,

B:  $\{(y, 1)\}$

# C-Set Merge

Machine A

Additions

A:  $\{(x, 2)\}$ ,  
B:  $\{(y, 1), (z, 2)\}$

Subtractions

A:  $\{(x, 1)\}$ ,  
B:  $\{(y, 1)\}$

Machine B

Additions

A:  $\{(x, 2)\}$ ,  
B:  $\{(y, 1), (z, 2)\}$

Subtractions

A:  $\{(x, 1)\}$ ,  
B:  $\{(y, 1)\}$

# C-Set Total

Machine A

Additions

A:  $\{(x, 2)\}$ ,  
B:  $\{(y, 1), (z, 2)\}$

Subtractions

A:  $\{(x, 1)\}$ ,  
B:  $\{(y, 1)\}$

Machine B

Additions

A:  $\{(x, 2)\}$ ,  
B:  $\{(y, 1), (z, 2)\}$

Subtractions

A:  $\{(x, 1)\}$ ,  
B:  $\{(y, 1)\}$

Set is  $\{x, z\}$



**C-Set allows  
elements to be  
added and removed  
many times**

**C-Set allows elements  
to be removed  
more times than  
they have been added**

# OR-Set

**Store element and  
unique token**

# OR-Set

## Machine A

### Additions

A:  $\{(x, \#a), (x, \#d)\}$ ,  
B:  $\{(y, \#b)\}$

### Subtractions

A:  $\{(x, \#a)\}$ ,  
B:  $\{\}$

## Machine B

### Additions

A:  $\{(x, \#a)\}$ ,  
B:  $\{(y, \#b), (z, \#c)\}$

### Subtractions

A:  $\{\}$ ,  
B:  $\{(y, \#b)\}$

# OR-Set Merge

## Machine A

### Additions

A:  $\{(x, \#a), (x, \#d)\}$ ,  
B:  $\{(y, \#b), (z, \#c)\}$

### Subtractions

A:  $\{(x, \#a)\}$ ,  
B:  $\{(y, \#b)\}$

## Machine B

### Additions

A:  $\{(x, \#a), (x, \#d)\}$ ,  
B:  $\{(y, \#b), (z, \#c)\}$

### Subtractions

A:  $\{(x, \#a)\}$ ,  
B:  $\{(y, \#b)\}$

# OR-Set Total

Machine A

Additions

A:  $\{(x, \#a), (x, \#d)\}$

B:  $\{(y, \#b), (z, \#c)\}$

Subtractions

A:  $\{(x, \#a)\}$ ,

B:  $\{(y, \#b)\}$

Machine B

Additions

A:  $\{(x, \#a), (x, \#d)\}$ ,

B:  $\{(y, \#b), (z, \#c)\}$

Subtractions

A:  $\{(x, \#a)\}$ ,

B:  $\{(y, \#b)\}$

Set is

$\{x, z\}$

**OR-Set *works* the  
way we expect**

**From sets, build**  
**trees, graphs,**  
**etc.**



# **CRDTS vs** **The Real** **World**

# **Strong Consistency**

## **Memory Usage**

### **Code**

# Strong Consistency

**Don't** build your  
billing platform on  
CRDTs

# Memory

# Usage

## Tombstones

## Machine IDs

# **Tombstones: Establish causal order and delete (Bieniussa et al. 2012)**

**Tombstones: Prune  
with heuristics  
(often based on  
time)**

**Machine IDs: OR-Sets**  
**don't** need them



**Machine IDs: Hierarchical  
organisation allows  
pruning  
(Almeida & Baquero.  
2013)**

# Code

## Riak 2.0

### Various open source libraries

The background of the image is a dramatic sunset sky with vibrant orange, yellow, and purple clouds. In the foreground, a large black silhouette of a dinosaur, resembling a T-Rex, is shown in profile, facing right. A smaller black silhouette of a cowboy wearing a hat and riding a horse is positioned on the dinosaur's back, also facing right. The text is overlaid on this scene.

Thank you!  
Now go forth and  
**DISTRIBUTE!**

<http://stjost.deviantart.com/art/Stomping-Off-Into-the-Sunset-277086274>

**More:**

**noelwelsh.com**