

One morning...



Why!?!?

# Practical Probabilistic Programming (With Cats)

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Explain what probabilistic programming is, for programmers

Show that all our  
favourite FP tricks apply

Work out what is bringing  
all the cats to the yard

# Science 1



Build a model



Milkshake



Fish



Nothing



60%



10%



30%

# Probability distribution

Dist[Enticement]



10%



20%

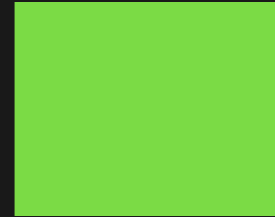
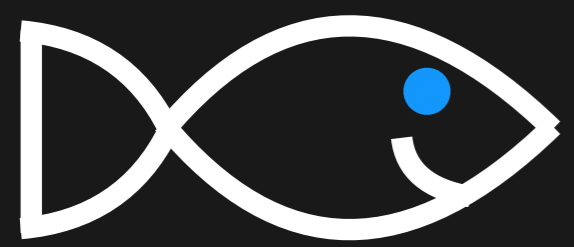


70%





20%



40%



40%



60%



30%



10%



# Conditional probability distribution

Enticement =>  
Dist[Cats]

Dist[E] ??? E => Dist[Cats] =  
Dist[Cats]

Dist[E] flatMap E => Dist[Cats] =  
Dist[Cats]

There is a monad for  
probability

Challenge question: if the monad represents conditional probability, what does the applicative represent?



#2  
Engineering

Implement the model  
and answer queries

Given there are 3 cats in the yard, what is the probability there is milkshake?

$$P(\textit{enticement} = \textit{milkshake} | \textit{cats} = 3)$$

Dist[(Enticement,  
Cats)]

Small discrete problems  
can be solved exactly

The general case requires  
approximate solutions

**Sampling** is a general method for calculating approximate solutions



Separate description of  
model from sampling  
process

User can interactively  
choose number of samples

Sampling method can  
be tailored to problem

Separate description of  
model from sampling  
process

Separate **abstract syntax**  
**tree** from **interpreter**

Reify monad as  
abstract syntax tree

The free monad!

Sampling is an **interpreter**  
for the free monad in the  
usual way.



# #3 Extensions

Condition distribution  
on observations

# Bayesian inference

# Composition of inference algorithms

# Distributing computation over a cluster

Probabilistic  
programming is an open  
area of research

# #4 Conclusions

There is a monad for  
probability



This is the basis for  
probabilistic programming

Reducing the cost of  
probabilistic inference has  
many benefits

Identify objects in deep  
space

# Analysis of gene sequencing experiments

Better targeting of  
online ads

Functional programming is  
extremely relevant for  
probabilistic programming

Code: [github.com/  
noelwelsh/pfennig](https://github.com/noelwelsh/pfennig)

# Thank You

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<https://github.com/noelwelsh/pfennig>

